*i-Ready Classroom Mathematics* lessons consist of three types of sessions: Explore, Develop, and Refine. The following is a walkthrough of the planning and support features within the Teacher's Guide for a Develop session. You will find many of the same features in the Explore and Refine sessions.



**Pacing Guide** session-by-session pacing is used to plan daily instruction and practice.

Additional Practice is for use as in-class small group work, after class work, or at-home learning.



<b>Purpose</b> provides a roadmap of what
students will be learning and doing across
the session.

**Start** establishes a clear and accessible entry point for each session, engaging students mathematically with prerequisite content. It frequently is an opportunity to have students engage in a math talk.

## **Develop Academic Language**

provides language support for all students and is especially useful in helping EL students use and produce academic language.

## **Support Partner Discussion**

provides teachers with prompts to help students engage in meaningful peer discourse.

## **Make Sense of the Problem**

uses a language routine to help students understand the problem. See the Language Routines section on the Teacher Toolbox (under the Program Implementation tab) for suggestions on how to integrate language routines, teacher moves, and conversation tips during instruction.

## LESSON 14 | SESSION 3 **Develop**

## Purpose

- **Develop** strategies for estimating solutions for word problems involving decimal addition or subtraction.
- Recognize that a decimal sum or difference is reasonable if the actual answer is close to an estimate.





## Possible Solution

All have decimal number addends with sums equal to 7.

B, C, and D all have decimals parts in the hundredths.

A and D have decimal parts that are easier to work with.

**WHY?** Support students' facility with recognizing decimals that are easier to work with.

## DEVELOP ACADEMIC LANGUAGE

**WHY?** Deepen understanding about *estimate* and *estimation*.

**HOW?** Tell students that an *estimate* or an *estimation* is an approximation. Have students find the word *estimation* in Apply It problem 8 and paraphrase the sentence using *estimate*. Then ask When in your life can you use *estimation?* When in your life do you need an exact answer?

## **TRY IT**

## Make Sense of the Problem

Before students work on Try It, use **Say It Another Way** to help them make sense of the problem. Confirm that students understand that they are asked to both estimate and calculate the amount of liquid in the container and that they can use the estimate to see if their solution is reasonable.

## 281 Common Misconception

identifies misconceptions that lead to errors in understanding, which can then be addressed in whole class discussion as students are prompted to explain their reasoning.

SMP 1, 2, 4, 5, 6

evelon Usin	a Estimation with Decimals	SESSION 3 • • • •	
id and try to solve the	e problem below.		
obby is conductin iquid A and 3.65 li container.	g a science experiment. He has 3.74 liters of ters of Liquid B. He pours both liquids into		
ow much liquid is ell if your answer i	in the container? Estimate and solve. s reasonable.		
rry It		Ath Toolkit	
Possible student wo	rk:	<ul> <li>base-ten blocks</li> </ul>	
Sample A		<ul> <li>base-ten grid paper</li> </ul>	
		decimal grids     pumber lines	
stimate:	Actual sum:	thousandths decimal	
ooth about 4.0.		place-value charts	
1 + 4 = 8	3.74 + 3.65 = (3.0 + 0.7 + 0.04) + (3.0 + 0.0	6 + 0.05)	
	= 3.0 + 3.0 + 0.7 + 0.6 + 0.04 +	+ 0.05	
	= 6 + 1.3 + 0.09		
The container has 7.	39 liters of liquid. Since 7.39 is close to 8.0, my		
Comple P			
interestor	A stud sum:		
sumate:	Actual sum:	$\cap$	
3.74 and 3.65 round	ed to the		
nearest tenth are bo	oth 3.7. 3.74	DISCUSS IT	
<b>3.7</b> + <b>3.7</b> = ( <b>3.0</b> + <b>0</b> )	$.7) + (3.0 + 0.7) \qquad \frac{+ 3.65}{7.39}$	Ask your partner: Can you	
= 3.0 + 3.0	explain that again?		
= 6.0 + 1.4	4	Tell your partner: I agree	
= 7.4		with you about	
The container has 7.	39 liters of liquid. Since 7.39 is close to 7.4, my	because	

## **DISCUSS IT**

## **Support Partner Discussion**

Encourage students to use the term *about* when discussing estimated solutions. Support as needed with guestions such as:

SMP 2, 3, 6

ted.

- Why did you choose the estimation strategy you used?
- What operation did you use? Why?

**Common Misconception** Look for students who choose decimals that are still difficult to compute with when estimating. Ask: *What decimals are equivalent to benchmark fractions? What decimals might be easier to add or subtract with? Why?* Encourage students to choose numbers they can add mentally.

## Select and Sequence Student Strategies

- One possible order for whole class discussion:
- concrete models to show estimates and/or the sum
- drawings to show estimates and/or the sum
- number lines used to find estimates and/or the sum
- equations used to find estimates and/or the sum

## **Select and Sequence Student Solutions**

gives a range of possible strategies—from concrete to representational to abstract for use in monitoring student work and facilitating discourse. This information can be used to make decisions about which models and strategies to share and discuss as a class.

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## **Facilitate Whole Class Discussion**

Call on students to share selected strategies. Allow time for students to think by themselves before starting the discussion.

Guide students to **Compare and Connect** the representations. Remind students to suggest other reasons that they know the solution is correct or reasonable.

**ASK** How did you choose numbers for your estimate? **LISTEN FOR** Students should see that good estimates use numbers that are easy to add and close to the actual addends. They may round to the

ASK What strategy did you use to find the actual sum?

nearest whole number, tenth, or 0.25.

LISTEN FOR Student may describe a range of models and strategies based on place value and properties of operations.

## Picture It & Model It

If no student presented these models, have students analyze key features and then point out the ways each model represents:

- the addends in the problem
- a way to estimate the sum

ASK How do the decimal grids and number line model show the addends in the problem? LISTEN FOR The decimal grids use shading to show the whole number and hundredths in each number. The number line shows each addend as a point.

For the decimals grids, prompt students to think about how the picture supports estimating.

• How do decimal grids show whole numbers?

• Between which two whole numbers is each addend? • How do the grids show which whole number is closer

to the addend? For the number line model, prompt students

to consider how the labels support estimating.

- What does each tick mark on the number line represent? Which tick marks are labeled with numbers?
- Between which two labeled tick marks does the point for each addend lie?
- How can you tell if each addend is closer to 3.5 or to 4.0?

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Explore different ways to understand estimating with decimals.

Bobby is conducting a science experiment. He has 3.74 liters of Liquid A and 3.65 liters of Liquid B. He pours both liquids into a container.

How much liquid is in the container? Estimate and solve. Tell if your answer is reasonable

### PICTURE IT



3.74 An estimate of the sum is 4 + 4

The actual sum can be found by finding 3.74 + 3.65.

MODEL IT



```
An estimate of the sum is 3.5 \pm 3.5.
The actual sum can be found by finding 3.74 + 3.65.
```

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## DIFFERENTIATION | EXTEND

- Deepen Understanding Number Line Model
- Prompt students to consider how to use the number line model to look at the precision of the estimates in Picture It and Model It.

3.6

**ASK** Which sum, 4.0 + 4.0 or 3.5 + 3.5, produces an estimate closer to the actual sum 3.74 - 3.65? How could the number line help you decide?

**LISTEN FOR** You can estimate the sum using either 4 + 4 or 3.5 + 3.5. The number line shows that both 3.65 and 3.74 are closer to 3.5 than to 4.0. Because each addend is closer to 3.5, the sum 3.5 + 3.5, or 7.0, is a more precise estimate than the sum 4 + 4, or 8.

**Generalize** Is it always better to choose numbers closer to the actual addends when estimating? Think about the actual addends 3.74 and 3.65 again. What would be the pros and cons of using 3.7 + 3.7 for estimating instead of 3.5 + 3.5? Have students explain their reasoning. Listen for understanding that 3.7 + 3.7 would produce a closer estimate than 3.5 + 3.5, but that the sum 3.7 + 3.7 is not as easy to find with mental math.

Lesson 14 Add and Subtract in Word Problems

SMP 6

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**Ask/Listen for** are mathematical discourse questions followed by expected student responses that support and facilitate whole class discussion.

As students share their thinking, the discourse questions can be used to make connections between student approaches and different models and representations, prompt justifications and critiques of approaches and solutions, and check conceptual understanding.

## **Standards for Mathematical Practice (SMP)** are infused throughout the instructional model.

## Deepen Understanding is a

consistent opportunity to build conceptual understanding of a key lesson concept by extending mathematical discourse. The content connects a particular aspect of lesson learning to an SMP, showing how it looks in the classroom.

**Monitor and Confirm** 

**Understanding** is a way to ensure that students have made sense of mathematical learning goals.

## **Facilitate Whole Class Discussion**

provides a series of related discourse questions that illuminate the mathematical ideas of the lesson, prompting students to make connections and use that understanding to solve problems leading to abstract reasoning. These questions help students learn how to articulate a generalization of the mathematical concept.

## Hands-On Activities occur

consistently at strategic points in the lesson after teachers have acquired understanding of students' learning through observation and their work on questions in the Student Worktext. The activities support students who are unsure of the concept and are an opportunity for small group reteaching while other students work independently. Use of concrete objects lets students access understanding in a different way.

## LESSON 14 | SESSION 3

## Develop

### **CONNECT IT** SMP 2.4.5.6

- Remind students that one thing that is alike about all the representations is they show ways to replace the original addends with numbers that are easier to compute with.
- Explain that on this page, they will use those numbers to explain how to check the reasonableness of a decimal sum.

## Monitor and Confirm Understanding

- **2 and 4** Check for understanding that:
- the actual sum is 7.39 L
- if both addends in the estimated sum are greater than the actual addends, the estimated sum will also be greater than the actual sum
- if both addends in the estimated sum are less than the actual addends, the estimated sum will also be less than the actual sum

## **Facilitate Whole Class Discussion**

**1** and **3** Tell students that these problems will prepare them to provide the explanation required in problem 5.

Be sure students understand the problems by asking them to think about what numbers to use when estimating.

**ASK** Both problems ask why a number is good to use as an addend for an estimate of the sum. How can different numbers, 4 and 3.5, both be good numbers to use for an estimated sum for this problem?

LISTEN FOR Good numbers are ones that are close to the actual addends but easy to compute with. The numbers 4 and 3.5 are both close to 3.74 and 3.65 and are easy to add. Different numbers can be used for estimating.

5 Look for the idea that you should estimate with numbers close to the actual numbers in the problem to find an estimated sum or difference. Students should explain that if the actual sum or difference is close to their estimate, then the answer is reasonable.

6 **Reflect** Have all students focus on the strategies used to solve this problem. If time allows, have students share their preferences with a partner.

Lesson 14 Add and Subtract in Word Problems

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### CONNECT IT

Now you will use the problem from the previous page to help you understand how to estimate with decimals

SESSION 3 • • • 0

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- Look at Picture It. Why is 4 a good number to use for each addend in an estimated sum? Possible answer: Each addend is close to 4, and 4 is an easy number to
- Is the actual sum of the measures of Liquids A and B in Picture It less than or greater than the estimated sum? Why? Less than; Possible answer: The actual sum is 7.39 liters. The estimated sum is 8 liters. Each addend in the estimated sum is greater than the corresponding addend in the actual sum, so this will be a high estimate of the actual sum
- Look at Model It. Why is 3.5 a good number to use for each addend in an estimated sum?

Possible answer: Each addend is close to 3.5, and 3.5 is an easy num to use for adding.

Is the actual sum of the measures of Liquids A and B in Model It less than or greater than the estimated sum? Why? n: Possible a ver: The actual sum is 7.39 liters. The estimated sun

is 7 liters. Each addend in the estimated sum is less than the correspondir m, so this will be a low e in the actual su

5 Explain how you can check if a decimal sum or difference is reasonabl Possible answer: Estimate the sum or difference using numb ers near t actual decimals that are easier to compute with. Com , pare the actual ans nate. If the answer is close to the estin

## 6 REFLECT

Look back at your Try It, strategies by classmates, and Picture It and Model It. Which models or strategies do you like best for estimating with decimals? Explain.

Possible answer: I like using a number line because I can find numbers that

are close to the numbers that I am adding.

## DIFFERENTIATION | EXTEND

Hands-On Activity Use money to model estimating with decimals.

If students have difficulty estimating decimal sums and differences, then use this activity to relate decimal amounts to money.

Materials For each pair: play money (6 dollar bills, 15 dimes, 5 quarters)

- Display the problem 2.13 + 3.84. Tell students that they can estimate the sum by thinking about rounding amounts of money to find \$2.13 + \$3.84.
- Ask: What place value are you rounding to when you round to the nearest dollar? To the nearest dime? [ones; tenths] When you round to the nearest quarter, are you rounding to a place value? [No; you are rounding to the nearest  $\frac{1}{4}$  of a dollar.]
- Have students model an estimate for 2.13 + 3.84 using dollars and dimes. [5 dollars and 9 dimes, or 5.90] If needed, ask: Is \$2.13 closer to \$2.10 or \$2.20? Is \$3.84 closer to \$3.80 or \$3.90?
- Have students model an estimate for 2.13 + 3.84 using dollars and quarters. [5 dollars and 4 guarters, or 6 dollars; 6] If needed, ask: Is \$2.13 closer to \$2.00 or \$2.25? Is \$3.84 closer to \$3.75 or to \$4.00?
- Repeat for other decimal sums, such as 1.42 + 2.79 and 4.31 + 0.96.

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**Apply It** solutions at point of use give a correct response with explanations that include multiple approaches to solving the problem.

## Apply It •

For all problems, encourage students to think about whether a whole number or decimal would be better to use for estimating the sum or difference.

Estimate: 3 meters or other reasonable amount; Actual: 3.25 meters; See possible work on the Student Worktext page. Students may also use 16 - 12.5 = 3.5 as an estimate. When finding the actual difference, students may also count on from 12.6 to 15.85 to find how many more meters of fencing Carlos needs.

Zaila does not need to pick more apples; See possible explanation on the Student Worktext page.
 Explanations should include reasoning that supports whether an actual sum,
 2.56 + 1.18 + 2.79 = 6.53, needs to be found.

## CLOSE EXIT TICKET

9 See **Connect to Culture** to support student engagement.

Hugo does not have enough money; See possible work on the Student Worktext page. Students may also choose to find the actual sum, \$8.57 + \$2.34 + \$5.25 = \$16.16, to determine whether Hugo has enough money. Students' solutions should indicate understanding of:

- computing estimated or actual decimal sums
- choosing appropriate addends to use for estimating
- comparing numbers, including decimals

## APPLY IT

## Use what you just learned to solve these problems.

Carlos has 12.6 meters of garden fencing. He needs 15.85 meters to enclose his garden. How many more meters of fencing does Carlos need to buy?

**SESSION 3 • • •** •

	Estimate to tell if your solution is reasonable. Show your work. Possible student work		
	Estimate: 16 — 13 = 3 3.25 is close to 3. My answer is reasonable.	Solution:	
		15.85	
		<u>-12.60</u>	
		3.25	
	Carlos needs 3.25 meters	more of garden fencing.	

8 Zaila wants at least 6 kilograms of apples for a recipe. She picks a 2.56-kilogram bag of red apples, a 1.18-kilogram bag of green apples, and a 2.79-kilogram bag of yellow apples. Does Zaila need to pick more apples?

Use estimation only to decide. Then explain if you are confident in your estimate or if you need to find an actual sum. Show your work.

Students' reasons for estimating or finding actual sums may vary. Check that estimates are accurate. Possible student work: A low estimate for the sum is 2.5 + 1 + 2.5 = 6.0. Since the actual mass of each bag of apples is more than its estimate, Zaila will have more than 6 kilograms. I do not need to add the actual numbers.

- Zaila does not need to pick more apples.
- Hugo buys supplies to make masks for Mardi Gras. He has \$15 in his pocket. He chooses green material for \$8.57 and purple material for \$2.34. He also wants to buy a bag of gold bells for \$5.25. Does he have enough money? Estimate or find an exact answer to solve. Show your work.

I can use an estimate to figure out if Hugo has enough money. Even if I use a low estimate for each item, it comes out to 58 + 52 + 55 = 515. Since the actual price of each item is more than the estimate, I know that Hugo does not have enough money.

Hugo does not have enough money.

**Close: Exit Ticket** is a quick formative assessment of each day's learning and serves as an indicator of students' progress toward mastery or partial mastery of the learning goal of the session.

This is the last question on the Student Worktext page.

## **Error Alert** gives insight into misconceptions that can lead to errors in calculation and provides on-the-spot remediation.

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Lesson 14 Add and Subtract in Word Problems

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Error Alert If students say Hugo has enough money based on their estimate of \$15, then have them compare each addend in their estimated sum with the actual addends. Ask them to explain if their estimate is a low estimate or a high estimate. With a low estimate, discuss how the actual cost of the material for Hugo's mask is higher than \$15.

Additional Practice can be used as in-class small group work, after class work, or at-home learning.

**Solutions** are labeled as *Basic*, Medium, and Challenge to show the relative difficulty level in relation to the questions at hand or the standard in question. Use these to support independent practice or differentiation as needed.

## LESSON 14 | SESSION 3 **Additional Practice**

## **Problem Notes**

Assign Practice Using Estimation with Decimals as extra practice in class or as homework.

- 1 An estimate is enough; See a possible explanation on the student page. Basic
- 2 2.77 liters; Subtract the amount Latasha has, 2.73 liters, from the amount she wants to have, 5.5 liters Medium

## LESSON 14 SESSION 3 Name: **Practice Using Estimation with Decimals** Study the Example showing how to estimate a difference using decimal grids Then solve problems 1–4. EXAMPLE Latasha has 2.73 liters of apple cider. She wants to have about 5.5 liters for her party. About how much more cider does Latasha need? One way to estimate is to round to the nearest tenth 5.5 is given to the nearest tenth. 2.73 is about 2.7 -2 Latasha needs about 2.8 liters more of apple cide Look at the Example. Does this situation require an exact answer, or is the estimate enough? Explain. An estimate is enough; Possible answer: The problem says Latasha wants about, not exactly, 5.5 L of apple cider. 2 Suppose Latasha wants to have exactly 5.5 liters of apple cider for her party. How much more apple cider does she need? Show your work Possible student work: 5.5 - 2.0 = 3.53.5 - 0.7 = 2.82.80 - 0.03 = 2.77

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Cloud

Machine

Pizza

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Fluency & Skills Practice provides ongoing opportunities for students to accurately, flexibly, and efficiently practice mathematical procedures and operations. This can be used as in-class small group work, after-class work, or at-home learning. Student pages are available in the optional Fluency and Skills Practice Book or on Teacher Toolbox. Download PDFs or editable versions, or assign to any LMS, including Google Classroom.

## **Fluency & Skills Practice**

### Assign Using Estimation with Decimals 🚯

In this activity students use estimation in the context of realworld problems involving the addition or subtraction of decimals. Estimation is an efficient method of solving problems in real-world situations when an exact answer is not required, as when determining the rough sum or difference of costs between differently priced goods.

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## **Additional Practice Opportunities**

Latasha needs 2.77 liters more of apple cider.

include digital Learning Games, Interactive Practice, Cumulative Practice, and i-Ready Personalized Instruction.

- 3 a. Group plan; Students may estimate the cost of each individual plan as \$60 and add \$60 + \$60 for an estimate of \$120.
  - b. \$5.59; group; When finding the cost of two individual plans, students may also break apart decimals and combine whole numbers and decimals separately before combining results to find the sum. They may count on from the cost of the group plan to the cost of two individual plans to find the difference. Medium
- 4 Any combinations of berries except raspberries, blackberries, and blueberries (1.83 + 1.72 + 1.5); See the student page for possible student work. Look for explanations that support the given combination. Challenae

- Biego and Efia are looking at cell phone plans. They could share a group plan that costs \$119.95 per month, or they could each pay for an individual plan that costs \$62.77 per month.
  - a. Estimate which choice would cost less for Diego and Efia. Explain why. The group plan would cost less. Possible explanation: The individual plans cost more than \$60 each, so two individual plans would be more than \$120, which is greater than the cost of the group plan.
  - **b.** How much money could they save per month by paying for the choice that costs less instead of the choice that costs more? Show your work

1 2 5. 5 4

Possible student work: 62.77 + 62.77 125.54  $\frac{-119.95}{5.59}$ 

- Diego and Efia can save \$5.59 by choosing a(n) group plar Ahanu wants to make at least 4.5 pounds, but no more than 5 pounds, of berry salad. He finds a carton of raspberries that weighs 1.83 pounds, a carton of blueberries that weighs 1.5 pounds, a carton of blackberries that weighs 1.72 pounds, and a carton of strawberries that weighs 1.29 pounds. If Ahanu wants to use three different types of berries, what is one combination of cartons he could buy? Explain. Show your work. + 1.8 + 1.7 +1.3
- Solution Accept all co s except rasp
- blueberries (5.05 pounds). Possible answer: Ahanu could buy raspberries, blackberries, and strawberries. By estimating each weight to the nearest
- tenth of a pound, I found a total weight of 1.8 + 1.7 + 1.3 = 4.8. The
- estimated weight of these three cartons is 4.8 pounds, which is between
- 4.5 pounds and 5 pounds. 286

## **DIFFERENTIATION | ENGLISH LEARNERS**

## Levels 1–3: Reading/Writing

Use with Apply It problem 1. Read the problem aloud to students and ask them to circle the amount of blue paint and the amount of yellow paint. Have partners discuss the problem using these sentence frames:

- Rafael has \_\_\_\_ounces of blue paint.
- Rafael has \_\_\_\_\_ ounces of yellow paint.
- We need to find the amount of \_\_\_\_\_.

Ask students to circle the term exact answer. Remind students that exact answer means they must figure out the actual or precise answer. Have partners solve the problem. Then have them record if the answer makes sense using the sentence frame:

• Our answer makes sense because

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## Levels 2–4: Reading/Writing

Use with Apply It problem 1. Have students read the problem with a partner. Have partners identify important quantities in the problem, then ask: What are the two things you need to find? [an estimate and an exact answer] What do you need to explain? [how you know the answer is reasonable] Have students work independently then check with a partner. Then provide the following

- sentence frames for partners to use in discussion and writing:
- Our estimate for the green paint is \_\_\_\_\_ because \_\_\_\_

 Rafael makes exactly ounces of green paint. Our answer is reasonable because \_\_\_\_\_

### Use with Apply It problem 1. Have students read the problem with a partner and ask clarifying questions to make sure they understand the

Levels 3–5: Reading/Writing

Use with Session 4 Apply It

problem. Confirm by asking: What 3 things does the problem ask for? [an estimate, an exact answer, explanation why an answer is reasonable]. Then have students work independently on the problem. Partway through, remind them to show how they estimated, how they found the exact answer, and how they know the answer is reasonable. Next, have students meet with a partner to read the explanation of why their answer is reasonable. Encourage students to make any additions or revisions needed.

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## **DIFFERENTIATION | ENGLISH**

**LEARNERS** helps teachers scaffold or amplify language in the next session so English learners can access and engage with grade-level mathematics.