# TEACHER'S GUIDE Overview 

continued
> i-Ready Classroom Mathematics lessons consist of three types of sessions: Explore, Develop, and Refine. The following is a walkthrough of the planning and support features within the Teacher's Guide for a Develop session. You will find many of the same features in the Explore and Refine sessions.

## Lesson Overview provides

 information for use in planning whole class instruction, small group differentiation, and independent learning opportunities.Content Objectives identify the mathematical learning goals for the lesson, while Language Objectives indicate the language students are expected to understand and produce as they work on those goals.

Prior Knowledge are opportunities to monitor understanding and identify students' learning needs.

LESSON 12

## Overview | Multiplication and Division Facts

## STANDARDS FOR MATHEMATICAL PRACTICE (SMP)

SMP 1, 2, 3, 4, 5, and 6 are integrated into the Try-Discuss-Connect framework.* This lesson provides additional support for: 2 Reason abstractly and quantitatively.
5 Use appropriate tools strategically.
7 Look for and make use of structure.

* See page $1 q$ to learn how every lesson includes these SMP.


## Objectives

## Content Objectives

- Fluently multiply and divide within 100.
- Use fact families and the relationship between multiplication and division to find unknown whole numbers in multiplication and division equations.
- Solve word problems using equations with the unknown whole number in
different places in the equations.


## Language Objectives

- Understand and use lesson vocabulary to explain the relationship between multiplication, division, and fact families to find unknown whole numbers during partner and whole class discussion.
- Explain in writing how to solve word problems using equations with the unknown whole numbers in different places in the equations.
- Justify solution strategies and answer choices during partner discussions.

Prior Knowledge

- Understand the meaning of multiplication.
- Know basic multiplication facts for 0 through 10.
- Understand the meaning of division.
- Connect multiplication and division.

Math Vocabulary is defined in the context of lessons, and academic words can be explored using the Academic Vocabulary Routine.

Learning Progression sets context for the mathematics of the lesson, providing information on how the content fits across and within grade levels-what students previously learned, what they are learning now, and what they will be learning next.

In this lesson students use fact families and a multiplication table to solve multiplication and division problems and to write related multiplication and division facts. Students learn how to use the rows and columns in a multiplication table to find missing numbers in multiplication and division facts. Students then apply that understanding to finding the third number in fact families.

In Grade 3 multiplication is a major focus. Students also build a foundationa understanding of division and learn how the two operations are related. Students have learned these concepts in previous Grade 3 lessons.

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## Vocabulary

Math Vocabulary
fact family a group of related equations that use the same numbers, but in a different order, and two different operation symbols. A fact family can show the relationship between addition and subtraction or between multiplication and division.
multiplication table a table showing multiplication facts.

Review the following key terms.
division equation an equation with a division symbol and an equal sign. For example, $15 \div 3=5$.
factor a number that is multiplied.
multiplication equation an equation with a multiplication symbol and an equal sign. For example, $3 \times 5=15$.
product the result of multiplication.
quotient the result of division.
Academic Vocabulary
each every.
complete(verb) to finish.


# TEACHER＇S GUIDE Overview 

continued

Purpose provides a roadmap of what students will be learning and doing across the session．

Start establishes a clear and accessible entry point for each session，engaging students mathematically with prerequisite content．It frequently is an opportunity to have students engage in a math talk．

## LESSON 12｜SESSION 2 ■■ロロ

Develop
－Develop strategies for solving division problems．
－Recognize that a fact family uses the same 3 numbers to make related multiplication and division facts．

START
CONNECT TO PRIOR KNOWLEDGE

```
Always, Sometimes,Never
    A Multiples of 5 end in 1.
    B Multiples of }9\mathrm{ are even
    C Multiples of 2 end in 0, 2, 4, 6, or 8.
    D The product of a number and 1is that
```

Solutions
$A$ is never true.
$B$ is sometimes true.
C is always true.
D is always true.

WHY？Support students＇facility with multiplication facts．

## Develop Academic Language

 provides language support for all students and is especially useful in helping EL students use and produce academic language．
## Support Partner Discussion

provides teachers with prompts to help students engage in meaningful peer discourse．

## Make Sense of the Problem

 uses a language routine to help students understand the problem． See the Language Routines section on the Teacher Toolbox（under the Program Implementation tab）for suggestions on how to integrate language routines，teacher moves，and conversation tips during instruction．
## Lesson 12

## Develop Working with Division Facts

Read and try to solve the problem below．
Aki wants to make 5 sled dog teams．There are 40 sled dogs，and the teams must have the same number of dogs．She wants to find how many sled dogs to put on each team．Aki writes：

$$
40 \div 5=\square
$$

How many sled dogs should Aki put on each team？


## TRY IT

Possible student work：
Sample A
$5 \times 1=5$
$5 \times 2=10$
$5 \times 3=15$
$5 \times 4=20$
$5 \times 5=25$
$5 \times 6=30$
$5 \times 6=30$
$5 \times 7=35$
Fact Family
$\xrightarrow{5 \times 7=35} \longrightarrow \begin{array}{r}5 \times 8=40 \\ 5 \times 8=40\end{array}$
$5 \times 8=40 \quad 8 \times 5=40$
$40 \div 8=5$
$40 \div 5=8$
Aki should put 8 sled dogs on each team．
Sample B
$5,10,15,20,25,30,35,40$
$\begin{array}{llllllll}1 & 2 & 3 & 4 & 5 & 6 & 7 & \binom{8}{8}\end{array}$
8 sled dogs

## Math Toolki －counters －button <br> －cups <br> － 1 －centimeter grid paper <br> －multiplication models <br> $\cdot$－number lines



## DISCUSS IT

SMP 2，3，6， 7

## Support Partner Discussion

Encourage students to use the terms equal groups and quotient as they discuss． Support as needed with questions such as：
－What did you notice about your partner＇s strategy that is different than yours？
－Is there another way of looking at that？
－How could you use a fact family to find the number of sled dogs Aki needs？
Common Misconception Look for students who try to multiply $40 \times 5$ instead of dividing or using the multiplication facts $5 \times 8=40$ or $8 \times 5=40$ ．Ask students to explain their reasoning as to whether the answer will be greater than or less than 40 ．

Select and Sequence Student Strategies
One possible order for whole class discussion：
－drawing or modeling equal groups
－drawing a number line to skip－count
－skip－counting by fives without a model
－using a fact from the related fact family

## Common Misconception

identifies misconceptions that lead to errors in understanding，which can then be addressed in whole class discussion as students are prompted to explain their reasoning．

## Select and Sequence Student Solutions

gives a range of possible strategies－from concrete to representational to abstract－ for use in monitoring student work and facilitating discourse．This information can be used to make decisions about which models and strategies to share and discuss as a class．

## Facilitate Whole Class Discussion

Call on students to share selected strategies. Prompt students to tell how sure they are about their ideas and explain why. Guide students to Compare and Connect the representations. After each strategy, allow individual think time for students to process the ideas.
ASK Where does each model show the total number of dogs? The number of teams she wants to put together? The number of sled dogs to put on each team?
LISTEN FOR Students should recognize that accurate representations show that the total, 40 , is divided by 5 into 8 equal groups. Responses may include an equal-groups model, array, number line, skip-counting, and/or a fact family.

## Model It

If no student presented these models, have students analyze key features and then point out the ways each model represents

- the total number of dogs there are
the number of sled dog teams Aki wants
- the number of dogs on each team
- either division or multiplication

ASK What number tells the number of equal groups in the number line? In the fact family? What does that number represent?
LISTEN FOR 8 is the number of jumps or equal groups in the number line and the fact family. It represents the number of dogs on each team.

For a number line model, prompt students to identify the ending number on the number line and the length of the jumps used.

- How is the number line set up?
-Why is each jump by 5?
Why is the number of jumps counted?
For a fact family, prompt students to identify how knowing their multiplication facts can help them complete a fact family.
- How does knowing the multiplication facts for 5 help you to complete the fact family?
- What other multiplication facts could you use to help you complete the fact family?

Explore different ways to find the unknown number in a division fact.
Aki wants to make 5 sled dog teams. There are 40 sled dogs, and the teams must have the same number of dogs. She wants to find how many sled dogs to put on each team. Aki writes:

$$
40 \div 5=\square
$$

How many sled dogs should Aki put on each team?

## MODEL IT

You can use a number line to help you understand the problem.
Skip-count by fives to find the answer. Start at 0 and jump by fives until you get to 40 .


## MODEL IT

You can use fact families and multiplication facts you know.
Here are the facts in this family:

$$
5 \times 8=40 \quad 8 \times 5=40 \quad 40 \div 8=5 \quad 40 \div 5=8
$$

Write the multiplication facts for 5 :

| $1 \times 5=5$ | $2 \times 5=10$ | $3 \times 5=15$ | $4 \times 5=20$ | $5 \times 5=25$ |
| :--- | :--- | :--- | :--- | :--- |
| $6 \times 5=30$ | $7 \times 5=35$ | $8 \times 5=40$ | $9 \times 5=45$ | $10 \times 5=50$ |

Look for the fact that has the numbers you know from the fact family, 5 and 40 . Use that fact to fill in the unknown numbers above.

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## DIFFERENTIATION | EXTEND

$\square$
 Relate Multiplication and Division Facts

To support discussion of the fact family model, prompt students to consider the relationship between the numbers in a fact family.
Have students discuss how to know which fact family works for this problem. Write the equation $\square \times 5=40$ on the board.

ASK Where did this equation come from?
LISTEN FOR The missing number tells how many times you add 5 to get to 40 . It uses the same numbers as the equation in the problem, $40 \div 5=\square$.
Write the equation $5 \times \square=40$ on the board.
| ASK Where did this equation come from?
LISTEN FOR It is the same as $\square \times 5=40$, with the order of the factors switched.
Generalize Prompt students to see that you can write related multiplication facts for a division problem using the same numbers as the division facts. Both the division and multiplication facts tell the number of equal groups.

Ask/Listen for are mathematical discourse questions followed by expected student responses that support and facilitate whole class discussion.

As students share their thinking, the discourse questions can be used to make connections between student approaches and different models and representations, prompt justifications and critiques of approaches and solutions, and check conceptual understanding.

Standards for Mathematical
Practice (SMP) are infused throughout
the instructional model.

## Deepen Understanding is a

 consistent opportunity to build conceptual understanding of a key lesson concept by extending mathematical discourse. The content connects a particular aspect of lesson learning to an SMP, showing how it looks in the classroom.
# TEACHER＇S GUIDE Overview 

continued

## Monitor and Confirm

## Understanding is a way to ensure

 that students have made sense of mathematical learning goals．
## Facilitate Whole Class Discussion

provides a series of related discourse questions that illuminate the mathematical ideas of the lesson， prompting students to make connections and use that understanding to solve problems leading to abstract reasoning． These questions help students learn how to articulate a generalization of the mathematical concept．

## Hands－On Activities occur

 consistently at strategic points in the lesson after teachers have acquired understanding of students＇learning through observation and their work on questions in the Student Worktext． The activities support students who are unsure of the concept and are an opportunity for small group reteaching while other students work independently． Use of concrete objects lets students access understanding in a different way．
## LESSON 12｜SESSION 2 ■■ロロ

## Develop

## CONNECT IT

SMP 2，4，5， 7
－Remind students that one thing that is alike about all the representations is the numbers．
－Explain that on this page，students will use fact families to complete a division fact with an unknown in any position．

## Monitor and Confirm Understanding

（1）－2 Check for understanding that：
－the other division fact in the same family includes 45,5 ，and $\square$ ，but 5 and $\square$ switch places
－multiplication facts in the same family include 45， 5 ，and $\square$ ，but the factors 5 and $\square$ change order

## Facilitate Whole Class Discussion

3 Tell students that this problem will prepare them to provide the explanation required in problem 4.
Be sure students understand that the problem is asking them to select a multiplication fact from the table of multiplication facts for 5 in the second Model It on the previous page．
ASK How do you know which numbers to look for in the multiplication facts table？
LISTEN FOR A fact family uses the same three numbers in four related multiplication and division facts．So，a related multiplication fact will include 5 and 30 ．Only $6 \times 5=30$ includes 5 and 30 ．

0
Look for the idea that you need a fact in the same fact family，so the multiplication fact must use the same numbers as the division fact．

5eflect Have all students focus on the strategies used to solve this problem．If time allows， have students share their preferences with a partner．

## CONNECT IT <br> Now you will use the problem from the previous page to help you understand <br> how to use fact families to find an unknown number in a division fact． <br> （1）Clay wants to know how many sled dogs to put on each team if he uses 30 sled dogs to make 5 teams．He writes $30 \div \square=5$ ．What other division fact can he write to model this problem？ <br> $30 \div 5=\square$ <br> （2） <br> Write the two multiplication facts that are in the same fact family as Clay＇s division fact in problem 1．Use $\square$ for the unknown number． $5 \times \square=30$ and $\square \times 5=30$ <br> 3 Look at the list of multiplication facts for 5 on the previous page．Which fact will help Clay answer his division problem？How many sled dogs should <br> Clay put on each team？ <br> $6 \times 5=30$ ；Clay should put 6 sled dogs on each team． <br> （4） <br> Explain how you know which multiplication fact you can use to help you find the unknown number in a division fact． <br> Possible answer：You need to find a multiplication fact that has the same numbers that are given in the division problem． <br> （3）REFLECT <br> Look back at your Try It，strategies by classmates，and Model Its．Which models or strategies do you like best for finding unknown numbers in multiplication and division facts？Explain． <br> Some students may like skip－counting because they are comfortable with <br> it and can do it quickly．Others may prefer using fact families because they <br> know their multiplication facts and can easily find the missing third <br> number in a fact．

## DIFFERENTIATION｜EXTEND

## Hands－On Activity <br> Make fact triangle cards．

If students have trouble writing the division facts of a fact family，then use this activity to give a more concrete experience and practice writing division facts．

Materials For each pair： 10 triangles from Activity Sheet Multiplication Triangles（d） －Have students write out the multiplication facts for 6 （or other facts you wish students to practice）．Instruct them to circle the three numbers in each equation．
－Ask each pair to make a set of 10 triangle fact cards，one for each fact．For each card， have the students write the product in the top corner of the triangle and one of the factors in one of the other triangle corners．
－Have students practice their division facts by going through the cards，naming the missing factor，and then stating the related division fact with the missing factor，now the quotient of the division fact．The missing factor can be written on the back of each card．
－Repeat with facts for other numbers as time allows．

Apply It solutions at point of use give a correct response with explanations that include multiple approaches to solving the problem.

## Apply I

For all problems, encourage students to draw some kind of model to support their thinking.

6 6; See possible student work on the Student Worktext page.
(7) $2 \times 3=6 ; 3 \times 2=6$;
$6 \div 2=3 ; 6 \div 3=2$
The last three facts may be written in any order.

## CLOSE EXIT TICKET

(8) $7 \times 3=21 ; 3 \times 7=21$

Facts may be written in any order.
Students' solutions should indicate understanding of:

- how to write related multiplication and division facts from the same fact family
- how multiplication facts can be used to solve a division problem
Error Alert If students write multiplication facts that include 3 or 7 but are not in the same fact family, then have them make a multiplication facts for 3 table and then select the multiplication fact that includes both numbers used in the division problem.


## APPLY IT

Use what you just learned to solve these problems.
(6) Use the number line to solve $24 \div 4=\square$.

Show your work.
Possible student work:


Close: Exit Ticket is a quick formative assessment of each day's learning and serves as an indicator of students' progress toward mastery or partial mastery of the learning goal of the session.

This is the last question on the Student Worktext page.

Error Alert gives insight into misconceptions that can lead to errors in calculation and provides on-the-spot remediation.

# TEACHER'S GUIDE Overview 

Additional Practice can be used as in-class small group work, after class work, or at-home learning.

Solutions are labeled as Basic, Medium, and Challenge to show the relative difficulty level in relation to the questions at hand or the standard in question. Use these to support independent practice or differentiation as needed.

Fluency \& Skills Practice provides ongoing opportunities for students to accurately, flexibly, and efficiently practice mathematical procedures and operations. This can be used as in-class small group work, after-class work, or at-home learning. Student pages are available in the optional Fluency and Skills Practice Book or on Teacher Toolbox. Download PDFs or editable versions, or assign to any LMS, including Google Classroom.

## LESSON 12 |SESSION $2 \quad \square \square \square \square$

## Additional Practice

## Problem Notes

Assign Practice Working with Division Facts as extra practice in class or as homework.
(1) $3 \times 5=15$ or $5 \times 3=15$; 15 fish

- Basic

2. $15 \div 3=5 ; 5$ fish

Basic
(3) $15 \div 5=3 ; 3$ rows

Basic
(4) $4 \times 9=36$;
$9 \times 4=36$;
$36 \div 4=9$;
$36 \div 9=4$
Pairs of equations may be written in any order. Medium

Name: $\qquad$ LESSON 12 SESSION 2

## Practice Working with Division Facts

Study the Example showing how a picture can help you understand division facts. Then solve problems 1-9.


Write one of the facts from the list above that can help you solve problems 1-3.

1. How many fish are there altogether? $3 \times 5=15$ or $5 \times 3=15 ; 15$ fish
2. 15 fish swim in 3 equal rows. How many fish are in each row? $15 \div 3=5 ; 5$ fish
3) 15 fish swim in rows of 5 fish. How many rows of fish are there? $15 \div 5=3 ; 3$ rows
4. You know that $4 \times 9=36$. Write the whole fact family Use the numbers 4,9 , and 36 .
$4 \times 9 \times 36$
$9 \times 4 \times 36$
$36 \div 4=4$

## Fluency \& Skills Practice



Additional Practice Opportunities
include digital Learning Games,
Interactive Practice, Cumulative Practice, and i-Ready Personalized Instruction.
5) $\mathrm{C} ; 18 \div 2=9$

Medium
$18 \div 6=3 ; 18 \div 3=6$
Equations may be written in any order. Medium3 friends; See Student Worktext page for possible student work. Medium
(8) $24 \div 8=3 ; 24 \div 3=8$ Equations may be written in any order. Medium9) $8 \times 3=24 ; 3 \times 8=24$

Equations may be written in any order. Medium

## LESSON 12 SESSION 2

(5) Anwar draws 18 squares in two equal groups of 9 . Which division equation does his drawing show? (A) $9 \div 3=3$
(B) $18 \div 6=3$
(C) $18 \div 2=9$
(D) $6 \div 2=3$
(6)

## 

Pala has 24 trading cards. He gives away all his cards to friends. He gives 8 cards to each friend. Use this information to solve problems 7 - 9 .
(1) Use the number line to show how you can find how many friends Pala gave cards to.


Solution Pala gave cards to 3 friends.
(8) Write two different division facts for the story.
$24 \div 8=3 \quad$ and $\quad 24 \div 3=8$
(9) Write the multiplication facts that belong to the same fact family.

DIFFERENTIATION | ENGLISH
LEARNERS helps teachers scaffold or amplify language in the next session so English learners can access and engage with grade-level mathematics.

